



# Oasys GSA

Slab Design – RCSlab

### Oasys Your ideas brought to life

13 Fitzroy Street London W1T 4BQ Telephone: +44 (0) 20 7755 3302 Facsimile: +44 (0) 20 7755 3720

Central Square Forth Street Newcastle Upon Tyne NE1 3PL Telephone: +44 (0) 191 238 7559 Facsimile: +44 (0) 191 238 7555

e-mail: oasys@arup.com Website: oasys-software.com



#### © Oasys 1985 - 2019

All rights reserved. No parts of this work may be reproduced in any form or by any means - graphic, electronic, or mechanical, including photocopying, recording, taping, or information storage and retrieval systems - without the written permission of the publisher.

Products that are referred to in this document may be either trademarks and/or registered trademarks of the respective owners. The publisher and the author make no claim to these trademarks.

While every precaution has been taken in the preparation of this document, the publisher and the author assume no responsibility for errors or omissions, or for damages resulting from the use of information contained in this document or from the use of programs and source code that may accompany it. In no event shall the publisher and the author be liable for any loss of profit or any other commercial damage caused or alleged to have been caused directly or indirectly by this document.

# Contents

Acknowledgements	1
Introduction	1
Data requirements	1
RCSlab analysis procedure	4
Inclusion of moments resulting from additional and minimum eccentricities	4
Distribution of reinforcement	5
Concrete code related data	7
Codes with strength reduction factors	7
Current codes with partial safety factors on materials	12
Superseded codes with partial safety factors on materials	19
Current tabular codes	24
Codes with resistance factors on materials	31

# Acknowledgements

The theory and algorithms for slab design in GSA were developed in Arup by lan Feltham, and documented in an internal Arup publication. This document is based on that and reproduced here with permission.

# Introduction

*RCSlab* is a design postprocessor within GSA for reinforced concrete two-dimensional elements of uniform thickness subject to any combination of in-plane axial or shear force and out-of-plane bending moment and torsion. The calculations can be made following the principles of the most commonly used concrete codes. *RCSlab* is unable to allow for out-of-plane shear and through-thickness forces.

The input to the postprocessor comprises applied forces and moments, section depth, reinforcement positions, and material properties. The reinforcement orientations can be in general directions, referred to as  $\theta_1$  and  $\theta_2$ , which need not be orthogonal. The results comprise either areas of reinforcement for each face of the section in the two specified directions, or else an indicator to the effect that *RCSlab* is unable to find a solution for the current data. Early versions of the program were known as RC2D.

## Data requirements

Each run of *RCSlab* obtains the following data in any consistent set of units from the GSA analysis or *RCSlab* design data as appropriate:

- $N_{xx}$  ultimate applied axial force per unit width in the x-direction
- N<sub>yy</sub> ultimate applied axial force per unit width in the y-direction
- M<sub>xx</sub> ultimate applied bending moment per unit width about the x-axis
- M<sub>yy</sub> ultimate applied bending moment per unit width about the y-axis
- N<sub>xy</sub> ultimate applied in-plane shear force per unit width
- M<sub>xy</sub> ultimate applied torsion moment per unit width
- e<sub>add</sub> additional eccentricity (e<sub>add</sub> > 0) considered as acting in both senses
- e<sub>min</sub> minimum eccentricity (e<sub>min</sub> > 0) considered as acting in both senses
- h section thickness (h > 0)
- $z_{t1}$  position of top reinforcement centroid in direction 1 (0 <  $z_{t1}$  < h/2)
- $z_{t2}$  position of top reinforcement centroid in direction 2 (0 <  $z_{t2}$  < h/2)
- $z_{b1}$  position of bottom reinforcement centroid in direction 1(-h/2 <  $z_{b1}$  < 0)

Slab Design – RCSlab

Z <sub>b2</sub>	position of bottom reinforcement centroid in direction 2 (-h/2 < $z_{b2}$ < 0)
$\theta_1$	angle of reinforcement in direction 1, anticlockwise with respect to x-axis
$\theta_2$	angle of reinforcement in direction 2, anticlockwise with respect to x-axis
$A_{st1,min}$	minimum top reinforcement to be provided in direction $1(0 < A_{st1,min})$
A <sub>st2,min</sub>	minimum top reinforcement to be provided in direction 2 ( $0 < A_{st2,min}$ )
$A_{sb1,min}$	minimum bottom reinforcement to be provided in direction 1 (0 < $A_{sb1,min}$ )
$A_{sb2,min}$	minimum bottom reinforcement to be provided in direction 2 (0 < $A_{sb2,min}$ )
$f_{cd}$	compressive design strength of concrete ( $f_{cd} > 0$ )
$f_{cd,t} \\$	compressive design strength of top layer of concrete ( $f_{cd} > 0$ )
$f_{cd,b}$	compressive design strength of bottom layer of concrete ( $f_{cd} > 0$ )
$f_{cdc}$	cracked compressive design strength of concrete ( $f_{cdc} > 0$ )
$f_{cdu}$	uncracked compressive design strength of concrete ( $f_{cdu} > 0$ )
$f_{cdt}$	tensile design strength of concrete ( $f_{cdt} > 0$ )
€ <sub>ctran</sub> S	compressive plateau concrete strain ( $\epsilon_{ctrans} \ge 0$ )
ε <sub>cax</sub>	maximum axial compressive concrete strain ( $\epsilon_{cax} \ge \epsilon_{ctrans}$ )
ε <sub>cu</sub>	maximum flexural compressive concrete strain ( $\epsilon_{cu} \ge \epsilon_{cax}$ )
β	proportion of depth to neutral axis over which rectangular stress block acts ( $\beta \leq$ 1)
(x/d) <sub>max</sub>	maximum value of x/d, the ratio of neutral axis to effective depth, for flexure: $(x/d)_{min} < (x/d)_{max} \le 0.5/[\beta(0.5 + min{zt1, zt2, -zb1, -zb2}/h)]$
Es	elastic modulus of reinforcement
$f_{yd}$	design strength of reinforcement in tension ( $f_{yd} > 0$ )
$f_{ydc}$	design strength of reinforcement in compression, $(f_{ydc} > 0)$
$f_{lim}$	maximum linear steel stress of reinforcement ( $f_{lim} > 0$ )
ε <sub>plas</sub>	yield strain of reinforcement in tension ( $\epsilon_{plas} > 0$ )
Eplasc	yield strain of reinforcement in compression ( $\epsilon_{plasc} > 0$ )
ε <sub>su</sub>	design value of maximum strain in reinforcement
$\phi_{\Delta}$	maximum permitted angle between applied and resulting principal stress

In addition, the program needs to know whether to use, where appropriate, the faster approach and, if so, what the maximum area of reinforcement so calculated should be before the rigorous approach is used.

Page 2

Within *RCSlab* the reinforcement positions are measured with respect to the midheight of the section, the positions being measured positively upwards. The reinforcement angles are specified with respect to the x-axis and measured positively in an anticlockwise direction looking from above. It should be noted that the concrete is assumed to have zero tensile strength in the analysis; the tensile strength, f<sub>cdt</sub>, is only used to calculate the compressive strength when tensile strains are present.

The results of each run consist of the required area of reinforcement, negative if tensile, in each direction in the top and bottom faces or an error flag indicating that a solution could not be found.

# RCSlab analysis procedure

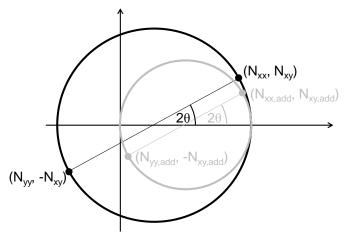
The following summarizes the procedure followed by RCSlab:

- 1. Adjust, where necessary, the applied moments for minimum eccentricities.
- 2. Split the section into three layers with the central layer unstressed and the outer layers taking in-plane stresses, the thicknesses corresponding to an acceptable neutral axis depth; calculate the stresses applied to each layer.
- 3. Calculate the stress to be taken by the concrete in each layer and the stress from each layer to be taken by reinforcement.
- 4. Calculate the force to be taken by each of the four sets of reinforcement (two faces, two directions) taking into account their positions relative to the layers.
- 5. Determine section strains compatible with the neutral axis depths implied by the layer thicknesses in 5.0.2 and the concrete strains in the outer layers from 5.0.3 for top and bottom layers.
- 6. Determine reinforcement strains compatible with the section strains.
- 7. From the strains, calculate the stress in each of the four sets of reinforcement.
- 8. Knowing the force to be taken by each of the four sets of reinforcement and the stress in each set of reinforcement, calculate the reinforcement areas required; these should not be less than the specified minimum values.
- 9. Repeat as necessary from 5.0.2, adjusting the layer thicknesses to achieve the minimum total area of reinforcement.
- 10. Where in-plane effects dominate, repeat from 5.0.2 adopting a model with the central layer stressed.
- 11. The design reinforcement areas correspond to the layer arrangement giving the minimum total area of reinforcement.
- 12. To speed up the calculation, an option is available to adopt a non-iterative technique where the loading is primarily either in-plane or out-of-plane. This approach is likely to lead to slightly more conservative results. The user can choose to use this approach in appropriate situations and can specify a total area of reinforcement, as a percentage of the cross-sectional area, above which a rigorous, iterative solution is used.

# Inclusion of moments resulting from additional and minimum eccentricities

The applied moments are adjusted to take into account the additional and minimum eccentricities of applied axial forces. The additional eccentricity, which can be used to model tolerances and second-order effects, is determined by the user; applied

bending moments are increased by compressive principal axial forces but are not adjusted for tensile principal axial forces. The components of in-plane force in the orthogonal directions for use with the additional eccentricity,  $N_{xx,add}$ ,  $N_{yy,add}$  and  $N_{xy,add}$ , are calculated assuming the angle between the principal direction and the x-axis is unchanged.



The default value of the minimum eccentricity, which can be overwritten, is taken from the chosen design code; this value, and all other code-dependent values, are given in Appendix 3. If the absolute value of the applied moment exceeds the sum of the additional and minimum eccentricity moments for Mxx, Myy and Mxy, then the applied moments are increased in magnitude by their respective additional moments. Otherwise two sets of applied moments are calculated, corresponding to eccentricities applied in the two senses.

Where  $|M + j.N_{add}.e_{add}| > |N.e_{min}|$ , the design moment  $M_d = M + j.N_{add}.e_{add}$ ;

otherwise,  $M_d = M + j.(N_{add}.e_{add} + N.e_{min})$  but restricted to the range -  $|N.e_{min}|$  to  $|N.e_{min}|$ 

For example, if the applied, additional and minimum eccentricity moments were 75kNm, 50kNm and 60kNm respectively, the design moments for the two sets would be 75-50-60 = -35kNm and 75+50 = 125kNm respectively. It should be noted that no specific allowance is made for slenderness.

## Distribution of reinforcement

*RCSlab* calculates the area of reinforcement required at each node. Since the reinforcement distribution corresponds to the force and moment distributions with their concentrations and peaks, there may be locations where no satisfactory reinforcement arrangement can be determined because the concrete is overstressed in shear. If these points, which are left black when contouring, are isolated, they can probably be ignored but larger areas will require changes to the geometry or material properties.

It is also usually appropriate to average values of reinforcement in areas of great change. For example, reinforcement requirements in flat slabs can be averaged over the central half of the column strips, the outer portions of the column strips and the middle strips, as when following code methods. It is hoped that future developments within GSA will help automate this averaging process.

### Concrete code related data

#### Codes with strength reduction factors

	ACI318-08	ACI318-11	ACI318-14	AS3600
Concrete strength	f <sub>c</sub> '	f <sub>c</sub> '	f <sub>c</sub> ′	f′c
Steel strength	fy	fy	fy	f <sub>sy</sub>
Strength reduction factor for axial compression* - $\phi_c$	φ = 0.65 [9.3.2.2]	φ = 0.65 [9.3.2.2]	φ = 0.65 [21.2.2]	φ = 0.6 [Table 2.2.2]
Strength reduction factor for axial tension* - $\phi_t$	φ = 0.9 [9.3.2.1]	φ = 0.9 [9.3.2.1]	φ = 0.9 [21.2.2]	φ = 0.8 (N bars) φ = 0.64 (L bars) [Table 2.2.2]
Uncracked concrete design strength for rectangular stress block f <sub>cdu</sub>	0.85fc′ [10.2.7.1]	0.85fc′ [10.2.7.1]	0.85fc′ [22.2.2.4.1]	α <sub>2</sub> f' <sub>c</sub> Where α <sub>2</sub> = 1.00-0.003f' <sub>c</sub> but within limits 0.67 to 0.85 [10.6.2.5(b)]
Cracked concrete design strength (equal to twice the upper limit on shear strength) f <sub>cdc</sub>	(5/3)√f <sub>c</sub> ' (f <sub>c</sub> ' in MPa) 20 √f <sub>c</sub> ' (f <sub>c</sub> ' in psi) [11.2.1.1 & 11.4.7.9]	1.66√f <sub>c</sub> ' (f <sub>c</sub> ' in MPa) <i>20 \f</i> c' ( <i>f</i> c' in psi_ [11.2.1.1 & 11.4.7.9 11.9.3]	1.66√fc' (fc' in MPa) 20 √fc′ (fc′ in psi) [11.5.4.3]	0.4f′c [11.6.2]

	ACI318-08	ACI318-11	ACI318-14	AS3600
Concrete tensile design strength (used only to determine whether section cracked) f <sub>cdt</sub>	(1/3)√f <sub>c</sub> ' (f <sub>c</sub> ' in MPa) <i>4 \f<sub>c</sub>' (f<sub>c</sub>' in psi)</i> [11.3.3.2]	0.33√f c' (fc' in MPa) 4 √ƒ c′ (fc′ in psi) [11.3.3.2]	0.33√f c' (fc' in MPa) 4 √f c′ (fc′ in psi) [22.5.8.3.3]	0.36√f′c [3.1.1.3]
Compressive plateau concrete strain <sub>Ectrans</sub>	0.002 [assumed]	0.002 [assumed]	0.002 [assumed]	0.002 [assumed]
Maximum axial compressive concrete strain <sub>ɛcax</sub>	0.003 [10.2.3]	0.003 [10.2.3]	0.003 [22.2.2.1]	0.0025 [10.6.2.2(b)]
Maximum flexural compressive concrete strain <sub>Ecu</sub>	0.003 [10.2.3]	0.003 [10.2.3]	0.003 [22.2.2.1]	0.003 [8.1.2.(d)]
Proportion of depth to neutral axis over which constant stress acts β	0.85-0.05(f <sub>c</sub> '-30)/7 (f <sub>c</sub> ' in MPa) 0.85- 0.05(f <sub>c</sub> '/1000-4) (f <sub>c</sub> ' in psi) but within limits 0.65 to 0.85 [10.2.7.3] β <sub>1</sub>	0.85-0.05(f <sub>c</sub> '-28)/7 (f <sub>c</sub> ' in MPa) 0.85- 0.05(f <sub>c</sub> //1000-4) (f <sub>c</sub> ' in psi) but within limits 0.65 to 0.85 [10.2.7.3] β <sub>1</sub>	0.85-0.05(f <sub>c</sub> '-28)/7 (f <sub>c</sub> ' in MPa) 0.85- 0.05(f <sub>c</sub> /1000-4) (f <sub>c</sub> ' in psi) but within limits 0.65 to 0.85 [22.2.2.4.3] β <sub>1</sub>	1.05-0.007f' <sub>c</sub> but within limits 0.67 to 0.85 [10.6.2.5(b)] γ

	ACI318-08	ACI318-11	ACI318-14	AS3600
Maximum value of ratio of depth to neutral axis to effective depth in flexural situations (x/d) <sub>max</sub>	 (1+0.004/ε <sub>cu</sub> ) [10.3.5] (c/d) <sub>max</sub>	 (1+0.004/ε <sub>cu</sub> ) [10.3.5] (c/d) <sub>max</sub>	 (1+0.004/ε <sub>cu</sub> ) [7.3.3.1 & 8.3.3.1] (c/d) <sub>max</sub>	0.36 [8.1.5] k <sub>u.max</sub>
Elastic modulus of steel	200GPa	200GPa	200GPa	200GPa
Es	[8.5.2]	[8.5.2]	[20.2.2.2]	[3.2.2(a)]
Design strength of reinforcement in tension f <sub>yd</sub>	f <sub>y</sub> [10.2.4]	f <sub>y</sub> [10.2.4]	f <sub>y</sub> [20.2.2.1]	f <sub>sy</sub> [3.2.1]
Design strength of reinforcement in compression f <sub>ydc</sub>	f <sub>y</sub> [10.2.4]	f <sub>y</sub> [10.2.4]	f <sub>y</sub> [20.2.2.1]	f <sub>sy</sub> [3.2.1]
Maximum linear steel stress	f <sub>y</sub>	f <sub>y</sub>	f <sub>y</sub>	f <sub>sy</sub>
f <sub>lim</sub>	[10.2.4]	[10.2.4]	[20.2.2.1]	[3.2.1]
Yield strain in tension	f <sub>y</sub> /E <sub>s</sub>	f <sub>y</sub> /E <sub>s</sub>	f <sub>y</sub> /E <sub>s</sub>	f <sub>sy</sub> /Es
	[10.2.4]	[10.2.4]	[20.2.2.1]	[3.2.1]
Yield strain in compression	f <sub>y</sub> /E <sub>s</sub>	f <sub>y</sub> /E <sub>s</sub>	f <sub>y</sub> /E <sub>s</sub>	f <sub>sy</sub> /E <sub>s</sub>
	[10.2.4]	[10.2.4]	[20.2.2.1]	[3.2.1]
Design strain limit	[0.01]	[0.01]	[0.01]	Class N         0.05           Class L         0.015           [3.2.1]         0.015
ε <sub>su</sub>	assumed	assumed	assumed	

	ACI318-08	ACI318-11	ACI318-14	AS3600
Maximum concrete strength	-	-	-	-
Maximum steel strength	-	-	-	f <sub>sy</sub> ≤ 500MPa [3.2.1]
Minimum eccentricity	0.10h [R10.3.6 & R10.3.7]	0.10h [R10.3.6 & R10.3.7]	0.10h [R22.4.2.1]	0.05h [10.1.2]
Minimum area compression reinforcement	-	-	-	1% (0.5% each face) [10.7.1 (a)]
maximum permitted angle between applied and resulting principal stress φ <sub>Δ</sub>	-	-	-	-

\*Applied forces and moments are divided by the strength reduction factor to obtain design values for use within RCSlab. The appropriate vales are determined as follows:

 $M = abs(M_{xx} + M_{yy})/2 + \sqrt{[(M_{xx} - M_{yy})^2/4 + M_{xy}^2]}$ 

 $N = (N_{xx} + N_{yy})/2 + \sqrt{[(N_{xx} - N_{yy})^2/4 + N_{xy}^2]}$ 

 $z_{min} = min\{z_{t1}, z_{t2}, -z_{b1}, -z_{b2}\}$ 

#### ACI318

#### AS3600

	$\mathbf{k}_{uc} = \mathbf{\varepsilon}_{cu} / (\mathbf{\varepsilon}_{cu} + \mathbf{f}_{yd} / \mathbf{E}_s)$	$k_{uc} = (1.19 - \phi_c) \times 12/13$
	$k_{ut} = \epsilon_{cu}/(\epsilon_{cu} + 0.005)$	$k_{ut} = (1.19 - \phi_t) \times 12/13$
	$M_c = \phi_c k_{uc} \beta f_{cdc} \times (1 - k_{uc} \beta/2) \times (h/2 + z_{min})^2 - N$	$\mathbf{k}_{ub} = \mathbf{\epsilon}_{cu}/(\mathbf{\epsilon}_{cu} + \mathbf{f}_{yd}/\mathbf{E}_s)$
× Zmin		$M_{c} = \phi_{c} k_{uc} \beta f_{cdc} \times (1 - k_{uc} \beta/2) \times (h/2 + z_{min})^{2} - min(0, N) \times z_{min}$
	$M_t = \phi_t k_{ut} \beta f_{cdc} \times (1 - k_{ut} \beta/2) \times (h/2 + z_{min})^2 - N \times$	$\mathbf{M}_{t} = \phi_{t} \mathbf{k}_{ut} \beta \mathbf{f}_{cdc} \times (1 - \mathbf{k}_{ut} \beta/2) \times (\mathbf{h}/2 + \mathbf{z}_{min})^{2} - \min(0, \mathbf{N}) \times \mathbf{z}_{min}$
Zmin		$N_b = \left[\phi_c k_{ub} \beta f_{cdc} \times (1 - k_{ub} \beta/2) \times (h/2 + z_{min})^2 - M\right] / z_{min}$

If $M \le M_t$ :	$\boldsymbol{\varphi}=\boldsymbol{\varphi}_t$	If $M \le M_t$ :	$\varphi_b=\varphi_t$	If $N \le 0$ : $\phi = \phi_b$	
If $M \ge M_c$ :	$\phi = \phi_{\rm c}$	If $M \ge M_c$ :	$\phi_b = \phi_c$	If $N \ge N_b$ :	$\phi = \phi_c$
Otherwise:	$\boldsymbol{\phi} = [(M_c \text{ - } M)\boldsymbol{\phi}_t + (M - M_t)\boldsymbol{\phi}_c]/(M_c - M_t)$	Otherwise:	$\phi_b = [(M_c - M)\phi_t + (M - M_t)\phi_c]/($	Otherwise:	$\phi = \phi_b (1 + \sqrt{[1 - 4(\phi_b - \phi_c) \times (N/N_b)]})$
		$M_c - M_t$ )		/ $\phi_b^2$ ] )/2	

#### Current codes with partial safety factors on materials

	EN1992-1-1 2004 +A1:2014	EN1992-2 2005	Hong Kong Buildings 2013	Hong Kong Structural Design Manual for Highways and Railways 2013	Indian concrete road bridge IRC:112 2011	Indian concrete rail bridge IRS 1997	Indian building IS456
Concrete strength	f <sub>ck</sub>	f <sub>ck</sub>	f <sub>cu</sub>	f <sub>ck,cube</sub>	f <sub>ck</sub>	f <sub>ck</sub>	f <sub>ck</sub>
Steel strength	f <sub>yk</sub>	f <sub>yk</sub>	fy	f <sub>yk</sub>	f <sub>yk</sub>	fy	fy
Partial safety factor on concrete	γc = 1.5 [2.4.2.4(1)]	γc = 1.5 [2.4.2.4(1)]	γ <sub>mc</sub> = 1.5 [Table 2.2]	γ <sub>c</sub> = 1.5 [5.1]	γc = 1.5 [A2.10]	γc = 1.5 [15.4.2.1(b)]	γ <sub>mc</sub> = 1.5 [36.4.2.1]
Partial safety factor on steel	γs = 1.15 [2.4.2.4(1)]	γs = 1.15 [2.4.2.4(1)]	γ <sub>ms</sub> = 1.15 [Table 2.2]	γ <sub>s</sub> = 1.15 [5.1]	γs = 1.15 [Fig 6.2]	γ <sub>m</sub> = 1.15 [15.4.2.1(d)]	γ <sub>ms</sub> = 1.15 [36.4.2.1]
Uncracked concrete design strength for rectangular stress block f <sub>cdu</sub>	$\label{eq:ccfck} \begin{split} f_{ck} &\leq 50 MPa \\ \alpha_{cc} f_{ck} > 50 MPa \\ (1 - (f_{ck} - 50)/200) \\ &\times \alpha_{cc} f_{ck} / \gamma_{C} \\ \alpha_{cc} \ is \ an \ NDP^{*} \\ [3.1.7(3)] \\ \eta f_{cd} \end{split}$	$\label{eq:ccfck} \begin{split} f_{ck} &\leq 50 MPa \\ \alpha_{cc} f_{ck} > 50 MPa \\ (1 - (f_{ck} - 50)/200) \\ &\times \alpha_{cc} f_{ck} / \gamma_{C} \\ \alpha_{cc} \ is \ an \ NDP^{*} \\ [3.1.7(3)] \\ \eta f_{cd} \end{split}$	0.67f <sub>cu</sub> /γ <sub>mc</sub> [Figure 6.1]	0.67f <sub>ck,cube</sub> /γc [Figure 5.3]	$\label{eq:fck} \begin{split} f_{ck} &\leq 60MPa \\ 0.67f_{ck}/\gamma c \\ f_{ck} &> 60MPa \\ (1.24-f_{ck}/250) \times \\ 0.67f_{ck}/\gamma c \\ [6.4.2.8 \ A2.9(2)] \\ \eta f_{cd} \end{split}$	0.60f <sub>ck</sub> /γ <sub>mc</sub> [15.4.2.1(b)]	0.67f <sub>ck</sub> / <sub>γmc</sub> [Figure 21]

	EN1992-1-1 2004 +A1:2014	EN1992-2 2005	Hong Kong Buildings 2013	Hong Kong Structural Design Manual for Highways and Railways 2013	Indian concrete road bridge IRC:112 2011	Indian concrete rail bridge IRS 1997	Indian building IS456
Cracked concrete design strength (equal to twice the upper limit on shear strength) f <sub>cdc</sub>	0.6×(1-f <sub>ck</sub> /250)× f <sub>ck</sub> /γc [6.2.2(6)] vf <sub>cd</sub>	0.312×(1-f <sub>ck</sub> /250 )× f <sub>ck</sub> /γc [6.109 (103)iii] (see also φ <sub>Δ</sub> ) vf <sub>cd</sub>	min{17.5, 2√[f <sub>cu</sub> ]} / <sub>γmc<sup>0.55</sup> [6.1.2.5(a)]</sub>	0.6× (1-0.8f <sub>ck,cube</sub> /250 )× 0.8f <sub>ck,cube</sub> /γc [5.1]	$\label{eq:relation} \begin{array}{l} f_{ck} \leq 80MPa \\ 0.6 \times 0.67 f_{ck} / \gamma_C \\ 80MPa < f_{ck} \leq \\ 100MPa  (0.9 - f_{ck} / 250) \times \\ 0.67 f_{ck} / 250) \times \\ 0.67 f_{ck} / \gamma_C \\ f_{ck} > 100MPa \\ 0.5 \times 0.67 f_{ck} / \gamma_C \\ [10.3.3.2] \\ v_1 f_{cd} \end{array}$	min {11.875, 1.875√[f <sub>ck</sub> ]}/ <sub>γmc<sup>0.55</sup> [15.4.3.1]</sub>	1.6√[f <sub>ck</sub> ] / γ <sub>mc</sub> 0.55 [Table 20]
Concrete tensile design strength (used only to determine whether section cracked) f <sub>cdt</sub>	$\label{eq:ct_constraint} \begin{array}{l} f_{ck} \leq 50MPa  \alpha \\ _{ct} \times 0.21 \; f_{ck}^{2/3}/\gamma_{C} \\ f_{ck} > 50MPa \\ \alpha_{ct} \times 1.48 \times \\ ln[1.8 + \; f_{ck}/10] \\ /\gamma_{C} \\ \alpha_{ct} \; is \; an \; NDP^{*} \\ [Table \; 3.1] \\ f_{ctd} \end{array}$	$\label{eq:ct_constraint} \begin{array}{l} f_{ck} \leq 50MPa  \alpha \\ {}_{ct} \times 0.21 \; f_{ck}{}^{2/3}/\gamma_{C} \\ f_{ck} > 50MPa \\ \alpha_{ct} \times 1.48 \times \\ ln[1.8 + \; f_{ck}/10] \\ /\gamma_{C} \\ \alpha_{ct} \; is \; an \; NDP^{*} \\ [Table \; 3.1] \\ f_{ctd} \end{array}$	0.36√[fcu]/ γmc [12.3.8.4]	f <sub>ck</sub> ≤ 60MPa [0.025f <sub>ck,cube</sub> + 0 .6] /γc f <sub>ck</sub> > 60MPa 2.1 /γc [Table 5.1]	$f_{ck} \le 60MPa \\ 0.1813 f_{ck}^{2/3} / \gamma_{C} \\ f_{ck} > 60MPa \\ 1.589 \times ln[1.8+ f_{ck}/12.5] / \gamma_{C} \\ [A2.2] \\ f_{ctd}$	0.36√[fck]/ γmc [16.4.4.2]	0.5√[f <sub>ck</sub> ]/ γ <sub>mc</sub> [From 6.2.2 (70% of SLS value / γ <sub>mc</sub> )]

	EN1992-1-1 2004 +A1:2014	EN1992-2 2005	Hong Kong Buildings 2013	Hong Kong Structural Design Manual for Highways and Railways 2013	Indian concrete road bridge IRC:112 2011	Indian concrete rail bridge IRS 1997	Indian building IS456
Compressive plateau concrete strain ɛctrans	$f_{ck} \le 50MPa \\ 0.00175 \\ f_{ck} > 50MPa \\ 0.00175+ \\ 0.00055\times \\ [(f_{ck}-50)/40] \\ [Table 3.1] \\ \epsilon_{c3}$	$f_{ck} \le 50MPa \\ 0.00175 \\ f_{ck} > 50MPa \\ 0.00175+ \\ 0.00055\times \\ [(f_{ck}-50)/40] \\ [Table 3.1] \\ \epsilon_{c3}$	0.002 [assumed]	[0.026f <sub>ck,cube</sub> + 1.1] /γc [5.2.6(1) & Table 5.1] εc2	$f_{ck} \le 60MPa$ 0.0018 $f_{ck} > 60MPa$ 0.00175+ 0.00055× [(0.8f_{ck}-50)/ 40] [Table 6.5 & A2.2] $\epsilon_{c3}$	0.002 [assumed]	0.002 [Figure 21]
Maximum axial compressive concrete strain ε <sub>cax</sub>	$f_{ck} \le 50MPa \\ 0.00175 \\ f_{ck} > 50MPa \\ 0.00175+ \\ 0.00055\times \\ [(f_{ck}-50)/40] \\ [Table 3.1] \\ \epsilon_{c3}$	$f_{ck} \le 50MPa \\ 0.00175 \\ f_{ck} > 50MPa \\ 0.00175+ \\ 0.00055\times \\ [(f_{ck}-50)/40] \\ [Table 3.1] \\ \epsilon_{c3}$	$f_{cu} ≤ 60MPa$ 0.0035 $f_{cu} > 60MPa$ 0.0035- 0.00006× $\sqrt{[f_{cu}-60]}$ [Figure 6.1]	[0.026f <sub>ck,cube</sub> + 1.1] /γc [5.2.6(1) & Table 5.1] εc2	$\label{eq:relation} \begin{array}{l} f_{ck} \leq 60 MPa \\ 0.0018 \\ f_{ck} > 60 MPa \\ 0.00175+ \\ 0.00055\times \\ [(0.8f_{ck}{-}50)/\ 40] \\ [Table \ 6.5\ \& \\ A2.2] \\ \epsilon_{c3} \end{array}$	0.0035 [15.4.2.1(b)]	0.002 [39.1a]

	EN1992-1-1 2004 +A1:2014	EN1992-2 2005	Hong Kong Buildings 2013	Hong Kong Structural Design Manual for Highways and Railways 2013	Indian concrete road bridge IRC:112 2011	Indian concrete rail bridge IRS 1997	Indian building IS456
Maximum flexural compressive concrete strain ε <sub>cu</sub>	$f_{ck} \le 50MPa \\ 0.0035 \\ f_{ck} > 50MPa \\ 0.0026+0.035\times \\ [(90-f_{ck})/ \ 100]^4 \\ [Table \ 3.1] \\ \epsilon_{cu3}$	$f_{ck} \le 50MPa \\ 0.0035 \\ f_{ck} > 50MPa \\ 0.0026+0.035 \times \\ [(90-f_{ck})/ \ 100]^4 \\ [Table \ 3.1] \\ \epsilon_{cu3}$	$f_{cu} ≤ 60MPa$ 0.0035 $f_{cu} > 60MPa$ 0.0035- 0.00006× $\sqrt{[f_{cu}-60]}$ [Figure 6.1]	$f_{ck,cube} \le 60MPa$ 0.0035 $f_{ck,cube} > 60MPa$ 0.0035- 0.00006× $\sqrt{[f_{ck,cube}-60]}$ [5.2.6(1)]	$f_{ck} \le 60MPa$ 0.0035 $f_{ck} > 60MPa$ 0.0026+0.035× $[(90-0.8f_{ck})/$ 100] <sup>4</sup> [Table 6.5 & A2.2] \$cu3	0.0035 [15.4.2.1(b)]	0.0035 [38.1b]
Proportion of depth to neutral axis over which constant stress acts β	$f_{ck} \le 50MPa$ 0.8 $f_{ck} > 50MPa$ 0.8-( $f_{ck}$ -50)/400 [3.1.7(3)] $\lambda$	$f_{ck} \le 50MPa$ 0.8 $f_{ck} > 50MPa$ 0.8-( $f_{ck}$ -50)/400 [3.1.7(3)] $\lambda$	$f_{cu} \le 45$ MPa 0.9 45 < $f_{cu} \le 70$ 0.8 $f_{cu} > 70$ MPa 0.72 [Figure 6.1]	$f_{ck,cube} \le 45MPa$ 0.9 $45 < f_{ck,cube} \le 70$ 0.8 $70 < f_{ck,cube} \le 85$ 0.72 [Figure 5.3]	$f_{ck} \le 60MPa$ 0.8 $f_{ck} > 60MPa$ 0.8-( $f_{ck}$ -60)/500 [A2.9(2)] $\lambda$	1.0 [15.4.2.1(b)]	0.84 [38.1c]
Maximum value of ratio of depth to neutral axis to effective depth in flexural situations (x/d) <sub>max</sub>	$f_{ck} \leq 50MPa$ (1- $k_1$ )/ $k_2$ $f_{ck} > 50MPa$ (1- $k_3$ )/ $k_4$ $k_1$ , $k_2$ , $k_3$ and $k_4$ are NDPs* [5.5(4)]	$f_{ck} \leq 50MPa$ (1- $k_1$ )/ $k_2$ $f_{ck} > 50MPa$ (1- $k_3$ )/ $k_4$ $k_1$ , $k_2$ , $k_3$ and $k_4$ are NDPs* [5.5(104)]	$f_{cu} \le 45MPa$ 0.50 $45 < f_{cu} \le 70$ 0.40 $f_{cu} > 70MPa$ 0.33 [6.1.2.4(b)]	$f_{ck} \leq 50MPa$ 0.344 $f_{ck} > 50MPa$ 0.6/{0.6 + 0.4/ (2.6 + 35[(90- f_{ck})/100]^4)} [5.1]	[upper limit]	$\frac{1}{(1+\epsilon_{s}/\epsilon_{cu})}$ where $\epsilon_{s} =$ 0.002 + f <sub>y</sub> /(E <sub>s</sub> $\gamma_{m}$ ) [15.4.2.1(d)]	fy = 250 0.53 fy = 415 0.48 fy = 500 0.46 [38.1f] x <sub>u.max</sub> /d

	EN1992-1-1 2004 +A1:2014	EN1992-2 2005	Hong Kong Buildings 2013	Hong Kong Structural Design Manual for Highways and Railways 2013	Indian concrete road bridge IRC:112 2011	Indian concrete rail bridge IRS 1997	Indian building IS456
Elastic modulus of steel	200GPa	200GPa	200GPa	200GPa	200GPa	200GPa	200GPa
Es	[3.2.7(4)]	[3.2.7(4)]	[Figure 3.9]	[5.1]	[6.2.2]	[Figure 4B]	[Figure 23B]
	Es	Es		Es	Es	Es	
Design strength of	fyk/γs	fyk/γs	fy/γms	fyk/γs	fyk/γs	fy/γm	fy/γms
reinforcement in tension	[3.2.7(2)]	[3.2.7(2)]	[Figure 3.9]	[5.1]	[6.2.2]	[Figure 4B]	[Figure 23B]
f <sub>yd</sub>	f <sub>yd</sub>	f <sub>yd</sub>			f <sub>yd</sub>		
Design strength of	f <sub>yk</sub> /γ <sub>s</sub>	f <sub>yk</sub> /γ <sub>s</sub>	f <sub>y</sub> /γ <sub>ms</sub>	f <sub>yk</sub> /γ <sub>s</sub>	f <sub>yk</sub> /γ <sub>s</sub>	(f <sub>y</sub> /γ <sub>m</sub> )/[1+	f <sub>y</sub> /γ <sub>ms</sub>
reinforcement in compression	[3.2.7(2)]	[3.2.7(2)]	[Figure 3.9]	[5.1]	[6.2.2]	(f <sub>y</sub> /γ <sub>m</sub> )/ 2000]	[Figure 23B]
fydc	f <sub>yd</sub>	f <sub>yd</sub>			f <sub>yd</sub>	[15.6.3.3]	
						f <sub>yc</sub> /γ <sub>m</sub>	
Maximum linear steel stress	f <sub>yk</sub> /γs	f <sub>yk</sub> /γs	f <sub>y</sub> /γ <sub>ms</sub>	fyk/γs	f <sub>yk</sub> /γs	0.8f <sub>y</sub> /γ <sub>m</sub>	fy/γms
flim	[3.2.7(2)]	[3.2.7(2)]	[Figure 3.9]	[5.1]	[6.2.2]	[Figure 4B]	[Figure 23B]
Yield strain in tension	f <sub>yk</sub> /(γsEs)	f <sub>yk</sub> /(γsEs)	f <sub>y</sub> /(γ <sub>ms</sub> E <sub>s</sub> )	fyk/(γsEs)	fyk/(γsEs)	f <sub>y</sub> /(γ <sub>m</sub> E <sub>s</sub> ) + 0.002	fy/(γmsEs)
εplas	[3.2.7(2)]	[3.2.7(2)]	[Figure 3.9]	[5.1]	[6.2.2]	[Figure 4B]	[Figure 23B]
Yield strain in compression	f <sub>yk</sub> /(γsEs)	f <sub>yk</sub> /(γsEs)	f <sub>y</sub> /(γ <sub>ms</sub> E <sub>s</sub> )	fyk/(γsEs)	fyk/(γsEs)	0.002	fy/(γmsEs)
8plasc	[3.2.7(2)]	[3.2.7(2)]	[Figure 3.9]	[5.1]	[6.2.2]	[assumed]	[Figure 23B]

	EN1992-1-1 2004 +A1:2014	EN1992-2 2005	Hong Kong Buildings 2013	Hong Kong Structural Design Manual for Highways and Railways 2013	Indian concrete road bridge IRC:112 2011	Indian concrete rail bridge IRS 1997	Indian building IS456
Design strain limit ε <sub>su</sub>	NDP <sup>*</sup> [ε <sub>ud</sub> ]	NDP* [ɛud]	(10β-1)×ε <sub>cu</sub> [6.1.2.4(a) (v)]	Grade 250 0.45 Grade 500B 0.045 Grade 500C 0.0675 [5.1(1) & 5.3(1) CS2:2012 Table 5 UKNA EN1992-1-1]	[0.01] assumed	[0.01] assumed	[0.01] assumed
Maximum concrete strength	f <sub>ck</sub> ≤ 90MPa [3.1.2(2)]	f <sub>ck</sub> ≤ 90MPa [3.1.2(2)]	f <sub>cu</sub> ≤ 100MPa [TR 1]	f <sub>ck,cube</sub> ≤ 85MPa [5.2.1(2)] C <sub>max</sub>	f <sub>ck</sub> ≤ 110MPa [A2.9(2)]	f <sub>ck</sub> ≤ 60MPa [Table 2]	f <sub>ck</sub> ≤ 80MPa [Table 2]
Maximum steel strength	f <sub>yk</sub> ≤ 600MPa [3.2.2(3)]	f <sub>yk</sub> ≤ 600MPa [3.2.2(3)]	f <sub>y</sub> = 500MPa [Table 3.1]	f <sub>yk</sub> ≤ 600MPa [5.1]	f <sub>yk</sub> ≤ 600MPa [Table 6.1]	-	f <sub>y</sub> ≤ 500MPa [5.6]
Minimum eccentricity	max{h/30, 20mm} [6.1(4)]	max{h/30, 20mm} [6.1(4)]	min{h/20, 20mm} [6.2.1.1(d)]	max{h/30, 20mm} [5.1]	0.05h [7.6.4.2]	min{0.05h, 20mm} [15.6.3.1]	max{h/30, 20mm} [25.4]
Minimum area compression reinforcement	-	-	-	-	-	-	-
Maximum permitted angle between applied and resulting principal stress φΔ	-	$ \theta - \theta_{el}  = 15^{\circ}$ [6.109 (103)iii] (see also f <sub>cdc</sub> )	-	-	-	-	-

\* NDPs are nationally determined parameters.

#### Superseded codes with partial safety factors on materials

Concrete Society R49	BS8110 1997 (Rev 2005) & Concrete Society TR49	BS5400 Part 4 & Concrete Society TR49	Hong Kong Buildings 2004 <sup>#</sup>	Hong Kong Buildings 2004 AMD1 2007	Hong Kong Highways 2006
cu	f <sub>cu</sub>	fcu	f <sub>cu</sub>	f <sub>cu</sub>	fcu
y	fy	fy	fy	fy	fy
	γ <sub>mc</sub> = 1.5 [2.4.4.1]	γ <sub>mc</sub> = 1.5 [4.3.3.3]	γ <sub>mc</sub> = 1.5 [Table 2.2]	γ <sub>mc</sub> = 1.5 [Table 2.2]	γ <sub>mc</sub> = 1.5 [4.3.3.3]
	γms = 1.15 [2.4.4.1]	γ <sub>ms</sub> = 1.15 [4.3.3.3]	γ <sub>ms</sub> = 1.15 [Table 2.2]	γ <sub>ms</sub> = 1.15 [Table 2.2]	γ <sub>ms</sub> = 1.15 [4.3.3.3]
	0.67f <sub>cu</sub> /γ <sub>mc</sub> [Figure 3.3]	0.60f <sub>cu</sub> /γ <sub>mc</sub> [5.3.2.1(b)]	0.67f <sub>cu</sub> /γ <sub>mc</sub> [Figure 6.1]	0.67f <sub>cu</sub> /γ <sub>mc</sub> [Figure 6.1]	0.60f <sub>cu</sub> /γ <sub>mc</sub> [5.3.2.1(b)]
- R 	<b>R49</b> μ hc = 1.5 .4.4.1] hs = 1.05 .4.4.1] 67f <sub>cu</sub> /γmc	R49Concrete Society TR49 $\mu$ $f_{cu}$ $\mu$ $f_{cu}$ $f_y$ $hc = 1.5$ $\gamma_{mc} = 1.5$ $.4.4.1]$ $[2.4.4.1]$ $hs = 1.05$ $\gamma_{ms} = 1.15$ $.4.4.1]$ $[2.4.4.1]$ $67f_{cu}/\gamma_{mc}$ $0.67f_{cu}/\gamma_{mc}$	R49Concrete Society TR49& Concrete Society TR49 $\mu$ fcufcu $f_{y}$ fcu $f_{y}$ fy $\mu_{c} = 1.5$ $\gamma_{mc} = 1.5$ $\mu_{c} = 1.05$ $\gamma_{ms} = 1.15$ $\mu_{s} = 1.05$ $\gamma_{ms} = 1.15$ $\mu_{c} = 1.15$ $(4.3.3.3)$ $(4.3.3.3)$ $(4.3.3.3)$ $67f_{cu}/\gamma_{mc}$ $0.60f_{cu}/\gamma_{mc}$	Ad9(Rev 2005) Concrete Society TR49Part 4 & Concrete Society TR49Buildings 2004# $\mu$ fcufcufcu $\mu$ fcufcu $\mu$ fcufcu $\mu$ fcufcu $\mu$ fyfy $\mu$ fy	porcrete Society R49(Rev 2005) Concrete Society TR49Part 4 & Concrete Society TR49Buildings 2004*Buildings 2004 AMD1 2007a $f_{cu}$ $f_{cu}$ $f_{cu}$ $f_{cu}$ $f_{cu}$ a $f_{cu}$ $f_{v}$ $f_{v}$ $f_{v}$ $f_{v}$ $f_{v}$ $h_{c} = 1.5$ $\gamma_{mc} = 1.5$ $\gamma_{mc} = 1.5$ $\gamma_{mc} = 1.5$ $.4.4.1$ $(2.4.4.1)$ $(4.3.3.3)$ $(Table 2.2)$ $(Table 2.2)$ $h_{v} = 1.15$ $\gamma_{ms} = 1.15$ $\gamma_{ms} = 1.15$ $\gamma_{ms} = 1.15$ $.4.4.1$ $(2.4.4.1)$ $(4.3.3.3)$ $(Table 2.2)$ $(Table 2.2)$ $67f_{cu}/\gamma_{mc}$ $0.67f_{cu}/\gamma_{mc}$ $0.60f_{cu}/\gamma_{mc}$ $0.67f_{cu}/\gamma_{mc}$ $0.67f_{cu}/\gamma_{mc}$

	BS8110 1997* & Concrete Society TR49	BS8110 1997 (Rev 2005) & Concrete Society TR49	BS5400 Part 4 & Concrete Society TR49	Hong Kong Buildings 2004 <sup>#</sup>	Hong Kong Buildings 2004 AMD1 2007	Hong Kong Highways 2006
Cracked concrete design strength (equal to twice the upper limit on shear strength) f <sub>cdc</sub>	2√[f <sub>cu</sub> ]/ γ <sub>mc<sup>0.55</sup> [3.4.5.2 &amp; TR 3.1.4]</sub>	2√[f <sub>cu</sub> ]/ γ <sub>mc<sup>0.55</sup> [3.4.5.2 &amp; TR 3.1.4]</sub>	min {11.875, 1.875√[f <sub>cu</sub> ]}/ γ <sub>mc<sup>0.55</sup> [5.3.3.3]</sub>	min{17.5, 2√[f <sub>cu</sub> ]} / <sub>γmc<sup>0.55</sup> [6.1.2.5(a)]</sub>	min{17.5, 2√[f <sub>cu</sub> ]} / <sub>γmc<sup>0.55</sup> [6.1.2.5(a)]</sub>	min {11.875, 1.875√[f <sub>cu</sub> ]}/ γ <sub>mc<sup>0.55</sup> [5.3.3.3]</sub>
Concrete tensile design strength (used only to determine whether section cracked) f <sub>cdt</sub>	0.36√[fcu]/ γmc [4.3.8.4]	0.36√[fcu]/ γmc [4.3.8.4]	0.36√[f <sub>cu</sub> ]/ γ <sub>mc</sub> [6.3.4.2]	0.36√[fcu]/ γmc [12.3.8.4]	0.36√[fcu]/ γmc [12.3.8.4]	0.36√[f <sub>cu</sub> ]/ γ <sub>mc</sub> [6.3.4.2]
Compressive plateau concrete strain <sub>Ectrans</sub>	0.002 [assumed]	0.002 [assumed]	0.002 [assumed]	0.002 [assumed]	0.002 [assumed]	0.002 [assumed]

	BS8110 1997 <sup>*</sup> & Concrete Society TR49	BS8110 1997 (Rev 2005) & Concrete Society TR49	BS5400 Part 4 & Concrete Society TR49	Hong Kong Buildings 2004 <sup>#</sup>	Hong Kong Buildings 2004 AMD1 2007	Hong Kong Highways 2006
Maximum axial compressive concrete strain ε <sub>cax</sub>	$f_{cu} \le 60MPa \ 0.0035$ $f_{cu} > 60MPa \ 0.0035$ $0.001 \times [(f_{cu}-60)/50]$ [TR49 3.1.3]	$f_{cu} \le 60MPa \ 0.0035$ $f_{cu} > 60MPa \ 0.0035$ $0.001 \times [(f_{cu}-60)/50]$ [TR49 3.1.3]	$f_{cu} \le 60MPa \ 0.0035$ [5.3.2.1(b)] $f_{cu} > 60MPa \ 0.0035$ $0.001 \times [(f_{cu}-60)/50]$ [TR49 3.1.3]	$f_{cu} ≤ 60MPa 0.0035$ $f_{cu} > 60MPa 0.0035$ - $0.00006 × \sqrt{[f_{cu}-60]}$ [Figure 6.1]	$f_{cu} ≤ 60MPa 0.0035$ $f_{cu} > 60MPa 0.0035$ - $0.00006 × \sqrt{[f_{cu}-60]}$ [Figure 6.1]	0.0035 [5.3.2.1(b)]
Maximum flexural compressive concrete strain ε <sub>cu</sub>	$f_{cu} \le 60MPa \ 0.0035$ $f_{cu} > 60MPa \ 0.0035$ $0.001 \times [(f_{cu}-60)/50]$ $[TR49 \ 3.1.3]$	$f_{cu} \le 60MPa \ 0.0035$ $f_{cu} > 60MPa \ 0.0035$ $0.001 \times [(f_{cu}-60)/50]$ [TR49 3.1.3]	0.0035 [5.3.2.1(b)]	$f_{cu} ≤ 60MPa 0.0035$ $f_{cu} > 60MPa 0.0035-$ $0.00006 × √[f_{cu}-60]$ [Figure 6.1]	$f_{cu} ≤ 60MPa 0.0035$ $f_{cu} > 60MPa 0.0035$ - $0.00006 × √[f_{cu}-60]$ [Figure 6.1]	0.0035 [5.3.2.1(b)]
Proportion of depth to neutral axis over which constant stress acts β	0.9 [Figure 3.3]	0.9 [Figure 3.3]	1.0 [5.3.2.1(b)]	0.9 [Figure 6.1]	$f_{cu} \le 45$ MPa 0.9 45 < $f_{cu} \le 70$ 0.8 $f_{cu} > 70$ MPa 0.72 [Figure 6.1]	1.0 [5.3.2.1(b)]

	BS8110 1997* & Concrete Society TR49	BS8110 1997 (Rev 2005) & Concrete Society TR49	BS5400 Part 4 & Concrete Society TR49	Hong Kong Buildings 2004 <sup>#</sup>	Hong Kong Buildings 2004 AMD1 2007	Hong Kong Highways 2006
Maximum value of ratio of depth to neutral axis to effective depth in flexural situations (x/d) <sub>max</sub>	[upper limit] (x/d) <sub>max</sub>	[upper limit] (x/d) <sub>max</sub>	$\frac{1}{1 + \epsilon_{s}/\epsilon_{cu}}$ ( where $\epsilon_{s} = 0.002 + f_{y}/(E_{s}\gamma_{ms})$ [5.3.2.1(d)] (x/d) <sub>max</sub>	$f_{cu} \le 45$ MPa 0.50 $45 < f_{cu} \le 70 0.40$ $f_{cu} > 70$ MPa 0.33 [6.1.2.4(b)] $(x/d)_{max}$	$f_{cu} \le 45$ MPa 0.50 $45 < f_{cu} \le 70 0.40$ $f_{cu} > 70$ MPa 0.33 [6.1.2.4(b)] $(x/d)_{max}$	$\frac{1}{(1+\epsilon_{s}/\epsilon_{cu})}$ where $\epsilon_{s} = 0.002 + f_{y}/(E_{s\gamma ms})$ [5.3.2.1(d)] (x/d)max
Elastic modulus of steel E <sub>s</sub>	200GPa [Figure 2.2]	200GPa [Figure 2.2]	200GPa [Figure 2] Es	200GPa [Figure 3.9]	200GPa [Figure 3.9]	200GPa [Figure 2] Es
Design strength of reinforcement in tension f <sub>yd</sub>	fy/γms [Figure 2.2]	f <sub>y</sub> /γ <sub>ms</sub> [Figure 2.2]	f <sub>y</sub> /γ <sub>ms</sub> [Figure 2]	fy/γms [Figure 3.9]	f <sub>y</sub> /γ <sub>ms</sub> [Figure 3.9]	fy/γ <sub>ms</sub> [Figure 2]
Design strength of reinforcement in compression f <sub>ydc</sub>	fy/γms [Figure 2.2]	fy/γms [Figure 2.2]	(fy/γms)/[1+ (fy/γms)/ 2000] [Figure 2]	fy/γ <sub>ms</sub> [Figure 3.9]	fy/γ <sub>ms</sub> [Figure 3.9]	(f <sub>y</sub> /γ <sub>ms</sub> )/[1+ (f <sub>y</sub> /γ <sub>ms</sub> )/ 2000] [Figure 2]

	BS8110 1997 <sup>*</sup> & Concrete Society TR49	BS8110 1997 (Rev 2005) & Concrete Society TR49	BS5400 Part 4 & Concrete Society TR49	Hong Kong Buildings 2004 <sup>#</sup>	Hong Kong Buildings 2004 AMD1 2007	Hong Kong Highways 2006
Maximum linear steel stress f <sub>lim</sub>	fy/γms [Figure 2.2]	fy/γms [Figure 2.2]	0.8fy/γms [Figure 2]	fy/γ <sub>ms</sub> [Figure 3.9]	fy/γ <sub>ms</sub> [Figure 3.9]	0.8fy/γ <sub>ms</sub> [Figure 2]
Yield strain in tension <sub>&amp;plas</sub>	f <sub>y</sub> /(γmsEs) [Figure 2.2]	f <sub>y</sub> /(γmsEs) [Figure 2.2]	f <sub>y</sub> /(γ <sub>ms</sub> E <sub>s</sub> ) + 0.002 [Figure 2]	f <sub>y</sub> /(γ <sub>ms</sub> E <sub>s</sub> ) [Figure 3.9]	f <sub>y</sub> /(γ <sub>ms</sub> E <sub>s</sub> ) [Figure 3.9]	f <sub>y</sub> /(γ <sub>ms</sub> E <sub>s</sub> ) + 0.002 [Figure 2]
Yield strain in compression <sub>Eplasc</sub>	f <sub>y</sub> /(γmsEs) [Figure 2.2]	f <sub>y</sub> /(γmsEs) [Figure 2.2]	0.002 [Figure 2]	f <sub>y</sub> /(γ <sub>ms</sub> E <sub>s</sub> ) [Figure 3.9]	f <sub>y</sub> /(γ <sub>ms</sub> E <sub>s</sub> ) [Figure 3.9]	0.002 [Figure 2]
Design strain limit ε <sub>su</sub>	(10β-1)×ε <sub>cu</sub> [3.4.4.1(e)]	(10β-1)×ε <sub>cu</sub> [3.4.4.1(e)]	([0.01] assumed	(10β-1)×ε <sub>cu</sub> [6.1.2.4(a)]	(10β-1)×ε <sub>cu</sub> [6.1.2.4(a)]	[0.01] assumed
Maximum concrete strength	f <sub>cu</sub> ≤ 100MPa [TR 1]	f <sub>cu</sub> ≤ 100MPa [TR 1]	-	f <sub>cu</sub> ≤ 100MPa [TR 1]	f <sub>ck</sub> ≤ 80MPa [Table 2]	-
Maximum steel strength	f <sub>y</sub> = 460MPa [Table 3.1]	f <sub>y</sub> = 500MPa [Table 3.1]	-	f <sub>y</sub> = 500MPa [Table 3.1]	f <sub>y</sub> = 500MPa [Table 3.1]	-
Minimum eccentricity	min{h/20, 20mm} [3.9.3.3]	min{h/20, 20mm} [3.9.3.3]	0.05h [5.6.2]	min{h/20, 20mm} [3.9.3.3]	min{h/20, 20mm} [6.2.1.1(d)]	0.05h [5.6.2]

	BS8110 1997* & Concrete Society TR49	BS8110 1997 (Rev 2005) & Concrete Society TR49	BS5400 Part 4 & Concrete Society TR49	Hong Kong Buildings 2004 <sup>#</sup>	Hong Kong Buildings 2004 AMD1 2007	Hong Kong Highways 2006
Minimum area compression reinforcement	-	-	-	-	-	-
maximum permitted angle between applied and resulting principal stress φ <sub>Δ</sub>	-	-	-	-	-	-

\* BS8110: 1985 is similar to BS8110: 1997 but with a value of 1.15 for  $\gamma_{\text{ms.}}$ 

# Hong Kong 1987 code is similar to BS8110: 1985.

#### Current tabular codes

	PR China GB 50010 2002
Characteristic concrete cube strength	f <sub>cu,k</sub> (value after 'C' in grade description)

	PR China GB 50010 2002
Characteristic steel strength	f <sub>yk</sub> – related to bar type in Table 4.2.2-1
Design concrete strength	$f_c - related to f_{cu,k}$ in Table 4.1.4
Uncracked concrete design strength for rectangular stress block f <sub>cdu</sub>	$\label{eq:fcu,k} \begin{split} f_{cu,k} &\leq 50 MPa \\ f_{c} \\ f_{cu,k} &> 50 MPa \\ [1 - 0.002(f_{cu,k}-50)] \times f_{c} \\ [7.1.3] \\ \alpha_{1}f_{c} \end{split}$
Cracked concrete design strength (equal to twice the upper limit on shear strength) f <sub>cdc</sub>	$\label{eq:relation} \begin{array}{l} f_{cu,k} \leq 50 MPa \\ 0.4f_c \\ f_{ck} > 50 MPa \\ 0.4 \times [1 - 0.00667(f_{cu,k} - 50)] \times f_c \\ [7.5.1] \\ 0.4\beta_c f_c \end{array}$

	PR China GB 50010 2002
Concrete tensile design strength (used only to determine whether section cracked) f <sub>cdt</sub>	f <sub>t</sub> - related to f <sub>cu,k</sub> in Table 4.1.4
Compressive plateau concrete strain	f <sub>cu,k</sub> ≤ 50MPa 0.002
Ectrans	f <sub>cu,k</sub> > 50MPa 0.02 + 0.5(f <sub>cu,k</sub> - 50)×10 <sup>-5</sup>
	[7.1.2]
	03
Maximum axial compressive	f <sub>cu,k</sub> ≤ 50MPa 0.002
concrete strain <sub>Ecax</sub>	f <sub>cu,k</sub> > 50MPa 0.02 + 0.5(f <sub>cu,k</sub> - 50)×10 <sup>-5</sup>
	[7.1.2]
	03

	PR China GB 50010 2002
Maximum flexural compressive concrete strain ɛcu	$f_{cu,k} \le 50MPa$ 0.0033 $f_{cu,k} > 50MPa$ $0.0033 - (f_{cu,k}-50) \times 10^{-5}$ [7.1.2] $\epsilon_{cu}$
Proportion of depth to neutral axis over which constant stress acts β	$f_{cu,k} \le 50MPa$ 0.8 $f_{cu,k} > 50MPa$ 0.8-0.002( $f_{cu,k}$ -50) $\beta_1$
Maximum value of ratio of depth to neutral axis to effective depth in flexural situations (x/d) <sub>max</sub>	β1/[1+fy/(Esεcu)] [7.1.4 & 7.2.1] ξ <sub>b</sub>

	PR China GB 50010 2002
Elastic modulus of steel	f <sub>y</sub> < 300MPa 210GPa
Es	f <sub>y</sub> ≥ 300MPa 200GPa
	[4.2.4]
	Es
Design strength of reinforcement in tension	f <sub>y</sub> – related to f <sub>yk</sub> in Table 4.2.3
f <sub>yd</sub>	
Design strength of reinforcement in compression	f' <sub>y</sub> – related to f <sub>yk</sub> in Table 4.2.3
fydc	
Maximum linear steel stress	f <sub>y</sub> – related to f <sub>yk</sub> in Table 4.2.3
flim	
Yield strain in tension	f <sub>y</sub> /E <sub>s</sub>
Eplas	

	PR China GB 50010 2002
Yield strain in compression <sub>&amp;plasc</sub>	f'y/Es
Design strain limit	0.01
ε <sub>su</sub>	[7.1.2(4)]
Maximum concrete	f <sub>cu,k</sub> ≤ 80MPa
strength	[Table 4.1.3]
Maximum steel	f <sub>yk</sub> ≤ 400MPa
strength	[Table 4.2.2-1
Minimum	max{h/30, 20mm}
eccentricity	[7.3.3]
Minimum area compression reinforcement	0.2% each face [Table 9.5.1]

	PR China GB 50010 2002
maximum permitted angle between applied and resulting principal stress	-
φΔ	

#### Codes with resistance factors on materials

	CSA A23.3-04	CSA A23.3-14	CSA S6-14
	Compulsory	Compulsory	Compulsory
	input	input	input
	parameters	parameters	parameters
Concrete strength	fc'	fc'	fc'
Steel strength	fy	fy	fy
	Code	Code	Code
	parameters	parameters	parameters
	that can be	that can be	that can be
	overwritten	overwritten	overwritten
Resistance factor on concrete	φ <sub>c</sub> = 0.65	φ <sub>c</sub> = 0.65	φ <sub>c</sub> = 0.75
	[8.4.2]	[8.4.2]	[8.4.6]
Resistance factor on steel	φ <sub>s</sub> = 0.85	φ <sub>s</sub> = 0.85	φ <sub>s</sub> = 0.9
	[8.4.3(a)]	[8.4.3(a)]	[8.4.6]
	Derived	Derived	Derived
	parameters	parameters	parameters
	that can be	that can be	that can be
	overwritten	overwritten	overwritten

	CSA A23.3-04	CSA A23.3-14	CSA S6-14
Uncracked concrete design strength for rectangular stress block	Max{0.67, 0.85-0.0015×f <sub>c</sub> '} ×фcf <sub>c</sub> '	Max{0.67, 0.85-0.0015×fc'} ×фcfc'	Max{0.67, 0.85-0.0015×fc'} ×φcfc'
f <sub>cdu</sub>	[10.1.7]	[10.1.7]	[8.8.3(f)]
Cracked concrete design strength (equal to twice the upper limit on shear strength) f <sub>cdc</sub>	0.5φ <sub>c</sub> f <sub>c</sub> ′ [11.3.3]	0.4\phi_f_c' [21.6.3.5]	0.5φ <sub>c</sub> f <sub>c</sub> ′ [8.9.3.3]
Concrete tensile design strength (used only to determine whether section cracked) f <sub>cdt</sub>	0.37¢c√[fc′] [22.4.1.2]	0.37¢c√[fc′] [22.4.1.2]	0.4ǫ <sub>c</sub> √[f <sub>c</sub> ′] [8.4.1.8.1]
Compressive plateau concrete strain <sub>Ectrans</sub>	0.002 [assumed]	0.002 [assumed]	0.002 [assumed]
Maximum axial compressive concrete strain ɛcax	0.0035 [10.1.3]	0.0035 [10.1.3]	0.0035 [8.8.3(c)]

	CSA A23.3-04	CSA A23.3-14	CSA S6-14
Maximum flexural compressive concrete strain ε <sub>cu</sub>	0.0035 [10.1.3]	0.0035 [10.1.3]	0.0035 [8.8.3(c)]
Proportion of depth to neutral axis over which constant stress acts β	Max{0.67, 0.97-0.0025×f <sub>c</sub> '} [10.1.7(c)] β1	Max{0.67, 0.97-0.0025×f <sub>c</sub> '} [10.1.7(c)] β1	Max{0.67, 0.97-0.0025×f <sub>c</sub> '} [8.8.3(f)] β1
Maximum value of ratio of depth to neutral axis to effective depth in flexural situations (x/d) <sub>max</sub>	[upper limit] (c/d) <sub>max</sub>	[upper limit] (c/d) <sub>max</sub>	[upper limit] (c/d) <sub>max</sub>
Elastic modulus of steel Es	φ <sub>s</sub> × 200GPa [8.5.3.2 & 8.5.4.1]	φ <sub>s</sub> × 200GPa [8.5.3.2 & 8.5.4.1]	<sub>φs</sub> × 200GPa [8.4.2.1.4 & 8.8.3(d)]
Design strength of reinforcement in tension f <sub>yd</sub>	φsfy [8.5.3.2]	φsfy [8.5.3.2]	¢sfy [8.4.2.1.4 & 8.8.3(d)]
Design strength of reinforcement in compression f <sub>ydc</sub>	φ₅fy [8.5.3.2]	φ₅fy [8.5.3.2]	∳₅fy [8.4.2.1.4 & 8.8.3(d)]

© Oasys Ltd 2015

Slab Design – RCSlab

	CSA A23.3-04	CSA A23.3-14	CSA S6-14
Maximum linear steel stress f <sub>lim</sub>	φsfy [8.5.3.2]	φsfy [8.5.3.2]	<sup>φsfy</sup> [8.4.2.1.4 & 8.8.3(d)]
Yield strain in tension	f <sub>y</sub> /E <sub>s</sub>	f <sub>y</sub> /E <sub>s</sub>	f <sub>y</sub> /E <sub>s</sub>
	[8.5.3.2]	[8.5.3.2]	[8.4.2.1.4]
Yield strain in compression I <sub>plasc</sub>	f <sub>y</sub> /E <sub>s</sub> [8.5.3.2]	f <sub>y</sub> /E <sub>s</sub> [8.5.3.2]	f <sub>y</sub> /E <sub>s</sub> [8.4.2.1.4]
Design strain limit	[0.01]	[0.01]	[0.01]
ε <sub>su</sub>	assumed	assumed	assumed
	Other	Other	Other
	parameters	parameters	parameters
Maximum concrete	fc' ≤ 80MPa	fc' ≤ 80MPa	f <sub>c</sub> ′ ≤ 85MPa
strength	[8.6.1.1]	[8.6.1.1]	[8.4.12]
Maximum steel strength	f <sub>y</sub> = 500MPa	f <sub>y</sub> = 500MPa	f <sub>y</sub> = 500MPa
	[8.5.1]	[8.5.1]	[8.4.2.1.3]
Minimum eccentricity	0.03h + 15mm	0.03h + 15mm	0.03h + 15mm
	[10.15.3.1]	[10.15.3.1]	[8.8.5.3(g)]

	CSA A23.3-04	CSA A23.3-14	CSA S6-14
Minimum area compression reinforcement	-	-	-